IWR, Heidelberg University

Exercise Sheet 3

Exercise 1: Matrix Class Implementation

(20 points)

Note: this exercise will form the foundation for several of the upcoming exercises, so if you want to work on only a subset of the sheet, it might be a good idea to start on this one.

In Scientific Computing the concept and use of matrices is crucial. Regardless of the field of expertise — if it is in optimization, statistics, artificial intelligence, or the solution of partial differential equations — we need matrices and solutions of linear systems of equations in nearly all applications.

In this exercise, we will implement a class Matrix in analogy to the class Vector from exercise sheet 1. Take care of the following points:

- (a) Class Matrix should have all functionality that class Vector has (constructors, methods, etc.).
- (b) The entries should be stored in a container of type std::vector<std::vector<double>>.
- (c) Instead of the number of elements int N in class Vector, class Matrix should contain the two numbers int numRows and int numCols that represent the number of rows and the number of columns respectively. Use numRows and numCols in all places where the member functions of class Vector used N, and re-implement the functionality adapted to the use of a class that represents matrix objects.
- (d) Use the member function double& operator()(int i, int j) for accessing the (i, j)-th element of objects of class Matrix.
- (e) Use the member function std::vector<double>& operator[](int i) to return the *i*-th row of a matrix object.
- (f) Class Matrix should have an additional constructor that constructs square matrices.

In addition to the member functions mentioned above, implement free functions that provide

- (g) the addition of two matrices,
- (h) the multiplication of a matrix with a scalar,
- (i) the multiplication of a scalar with a matrix,
- (j) a matrix-vector multiplication, where vectors are of type std::vector<double>,
- (k) a matrix-vector multiplication, where vectors are of type Vector.

Write a test program that tests all functionality of class Matrix (construction, the different kinds of multiplication, element access).

Exercise 2: Linked List

Using the simple example of a chained list we will practice the interaction of constructors, destructors and pointers.

We want to program a linked list which can store an arbitrary number of values of type **int**. Such a list consists of an object of class List, which refers to a sequence of objects of class Node. The list elements are stored in a component **int value** within each node, and a pointer Node* next points to the next node. The end of the list is designated by the pointer next having the value nullptr.

(10 points)

- (a) What is special about a pointer having the value nullptr?
- (b) Implement the class Node. Make sure that all member variables are always initialized, especially the next pointer.
- (c) Implement the class List with the following methods:

```
class List
1
   {
2
     public:
3
4
                                            // create an empty list
       List ();
5
       ~List ();
                                            // clean up list and all nodes
6
                                            // return pointer to first entry
       Node* first () const;
7
       Node* next (const Node* n) const; // return pointer to node after n
8
       void append (int i);
                                            // append a value to the end
9
       void insert (Node* n, int i);
                                           // insert a value before n
10
       void erase
                    (Node* n);
                                            // remove n from the list
11
   };
12
```

List must also store the beginning of the list, where would you place it in the class declaration? The next pointer of class Node should be private to ensure that the list structure isn't accidentally changed outside of class List. The member value is public to allow read and write access from outside the class. The line friend class List; has to be inserted into the declaration of the class Node to give the List class access to the next pointer. Additionally make sure that the destructor deletes all allocated Node objects.

(d) Test your implementation with the following program:

```
int main ()
1
   {
2
     List list;
3
     list.append(2);
4
     list.append(3);
5
     list.insert(list.first(), 1);
6
7
     for (Node* n = list.first(); n != 0; n = list.next(n))
8
        std::cout << n->value << std::endl;</pre>
9
   }
10
```

(e) What happens if one copies the list? And what happens if both lists are deleted?

```
int main ()
{
    Ist list;
    List list;
    list.append(2);
    ...
    List list2 = list;
    }
```